

# Theoretical analysis of the properties of composite materials and their use in improving the performance of mechanical structures

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## ABSTRACT

In mechanical engineering, composite materials are essential. Because of their complexity and multi-component makeup, they are among the most important technological advancements that have improved the performance of mechanical structures by striking a balance between strength, light weight, and longevity. Reviewing the theoretical analysis of composite material properties is the goal of this study, with particular attention paid to mechanical properties, classification models, and other features including thermal and environmental properties. The goal is to create a comprehensive knowledge base that aids in the creation of better structures. Using a literature and theoretical analysis methodology, the study examines the fundamental theories and mathematical models that describe how materials behave under different loading scenarios while accounting for the assumptions and constraints of each model. According to theoretical principles that explain the balance of strength, flexibility, and reliability, the results show how well some models predict the properties of composite materials and show how these properties can be used to design lightweight, high-strength structures. The creation of contemporary models and theories will successfully enhance the performance of structures and offer a sophisticated conceptual framework that will support the advancement of design procedures in the future and increase sustainability in engineering applications.

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## 1. Introduction

In the domains of materials science and mechanical engineering, composites represent a novel category. Due to technological developments, they are now a crucial feature of high-performance structure design, especially in the fields of civil engineering, automotive, and aerospace. Composite materials have special qualities that allow them to be used in applications that call for a lightweight yet robust construction. These qualities include being lighter than traditional materials, having a high resistance to loads and stresses, and being flexible [1].

The mechanical and environmental characteristics of composite materials have drawn increasing attention as a result of research and technical advancements over time. Instead of depending just on experimental testing and practical development, which are frequently expensive and time-consuming, it is now important to construct theoretical models in order to fully comprehend their behavior and analyze their performance. Apart from the difficulties in simulating how these materials behave under different load scenarios, more research is still required to fully comprehend their mechanical, thermal, and environmental characteristics as well as how they can enhance the functionality of mechanical structures composed of composite materials [2].

The comprehensive theoretical model that connects the fundamental properties, material behavior under various conditions, and engineering applications to ensure optimal structural design with the highest levels of efficiency and durability is clearly lacking, despite the fact that theoretical research in the field of composite materials has made a significant contribution to scientific advancement. The majority of recent research focuses on experimental or real-world applications, but more work needs to be done on the theoretical side to have a more thorough and in-depth knowledge of these materials' characteristics [3].

The goal of this study is to present a thorough theoretical investigation of composite materials' characteristics, emphasizing the theories and models that describe how they behave and how they can be used to enhance the functionality of mechanical structures. By examining theoretical and physical models that explain how composite materials behave under various load scenarios, this study also aims to lay the theoretical groundwork for future research on their characteristics. By supporting upcoming design and development procedures for materials and structures made of them, this seeks to advance mechanical engineering innovation and development.

## **2. Fundamentals of Composite Materials**

Composites are systems made up of many parts, preferably two distinct materials, that are joined to guarantee complimentary qualities, resulting in a material with better qualities than the parts alone. From a theoretical standpoint, composite materials are seen as asymmetric multicomponent systems whose behavior can only be streamlined by means of certain mathematical models. Theoretically, composite materials can be divided into several primary categories based on the characteristics of the constituents and how they interact, such as [4]:

- Matrix composites: These are made up of fundamental components (fibers), like glass or carbon fibers, that are bound together by a matrix.
- Fiber composites: The usage of high-performance fibers, intended to improve mechanical qualities, is what distinguishes these.
- Laminate composites: These are frequently utilized in applications needing high compressive and flexural resistance and are distinguished by their circular or oval shape.

### **2.1. Classification of Composite Materials Theoretically**

Within a theoretical framework based on the properties of the constituent materials, their interactions, their microstructure, and the unique performance characteristics that result, scientists and researchers categorize composite materials according to their engineering properties and constituent materials. The basis for classification is [5]:

- Structural arrangement: Composite materials with fibers organized either regularly or irregularly

- The nature of the matrix: glass, metal, or plastic, and how it affects the finished product's characteristics
- The way the components interact: as the potential use of multilayer structures or fiber adherence to the matrix.

## 2.2. Composite Material Components

Three primary components make up a composite material in theory, and each is examined independently of the application with an emphasis on their interactions and property analysis [6]:

- Matrix: serves as a tension control mechanism between the components, ties the fibers together, and aids in load distribution. It is seen as a flexible framework with certain stiffness and plasticity characteristics in theoretical models.
- Fibers: The fundamental unit responsible for a material's longevity and strength. They are categorized by type (glass, carbon, natural, etc.), and theoretical models that describe how stresses are distributed and released across the fibers under different loads are studied.
- Interface: the region that directly influences the material's reaction to load by joining the matrix to the fibers. To guarantee the stability and integrity of the composite material, the theoretical interaction between these media is investigated.

The theoretical underpinnings for mathematical models and theories that explain the behavior of composite materials are laid by an understanding of their structure and classification. Through integrated mathematical and theoretical models that precisely and transparently reflect mechanical, thermal, and environmental qualities, this is crucial for assisting with structural design and performance analysis [7].

## 3. Mechanical Properties of Composite Materials

A key component of the theoretical analysis of composite materials is an understanding of their mechanical characteristics. By using theoretical models and mathematical principles rather than actual practical testing, it seeks to forecast how the material will behave under different loads, such as tensile, compressive, or bending. The following important subjects are covered in this section to give a thorough understanding of the nature of composite materials' mechanical performance from a theoretical standpoint:

### A. The Use of Theory in Mechanical Property Prediction

The mechanical predictions of composite materials are based on mathematical models that use equations and hypotheses that support theoretical understanding and are based on the qualities of the fundamental components, such as fibers and matrix. Mathematical correlations between stress and strain are established by applying material and load laws and continuum mechanics principles. This explains how stresses are dispersed inside the composite material or how the different components interact under loading. These models are distinguished by their capacity to forecast characteristics like toughness, stiffness, and strength while accounting for the impacts of bending, torsion, and thermal expansion [8].

### B. Models for Moment and Flexural Analysis

The behavior of composite constructions of different sizes under mechanical loads is assessed using theoretical analysis models. The solid mechanics equations are used in this work, and crucial tools include differential equations that describe boundary states and bending. These formulas determine the distribution of stresses, bends, and moments while accounting for structural and

material characteristics. Additionally, it discusses the theoretical definition of stiffness and elasticity, emphasizing how member length, load type, and material composition affect structural performance [9].

#### C. Theoretical Examination of Ductility and Toughness

Ductility is the capacity of a material to undergo deformation without breaking, whereas toughness is the capacity of a material to bear stresses without failing. Mathematical models that investigate the limits at which elastic deformations shift to inelastic ones and estimate failure limits using mathematical equations derived from matrix and fiber properties serve as the theoretical embodiment of this idea. With the ability to characterize the behavior of the material during various phases of deformation and to assess its flexibility and resistance to abrupt or gradual changes in high or complex load instances, these models are predicated on assumptions about how the material's constituent parts deteriorate [10].

#### D. Resistance to Stress and Strain

Based on theoretical models that connect material qualities with engineering features, this field examines a collection of laws and theories that calculate the resistance of composite materials to stress and strain. The reaction of the material under load, failure modes, and factors influencing mechanical performance, such as matrix type, fiber type, and fiber arrangement, are all determined via theoretical stress and strain analysis. Analyzing how materials react to temporal behavior and the coexistence of various components during deformation, with an emphasis on interactions that impact overall strength and toughness, is another aspect of theoretical research [11].

The goal of the theoretical models and mathematical underpinnings is to offer a thorough comprehension of the mechanical behavior of composite materials. With the use of these theories, more effective mechanical structures may be created and designed, less realistic experimental testing is required, and precise forecasts of engineering performance under varied operating situations can be made.

### 4. Additional Composite Material Properties

Particularly from a theoretical standpoint grounded in scientific rules and data, the characteristics of composite materials are crucial elements that greatly impact their performance and applicability in engineering applications. In-depth discussions of the thermal and environmental characteristics, theoretical stability and behavior of composite materials, their durability, and the impact of external factors on their performance are covered in this section, with an emphasis on examining the theoretical underpinnings and models that account for these characteristics.

#### A. Environmental and Thermal Characteristics

This section examines how composite materials react to variations in temperature, stability over time, thermal conductivity, and radiation absorption. Theoretically, mathematical models based on the inherent characteristics of the matrix and fibers are used to characterize and forecast the thermal properties of composite materials, accounting for the interaction of these elements with meteorological conditions. Through a mathematical model based on differential equations that describe heat transfer and expansion, for instance, the performance of the material can be assessed in harsh environments. Heat transfer theory and thermal expansion theory are used to predict changes in properties with changing conditions [13].

#### B. A Theoretical View of Stability and Electrostatics

One significant factor influencing composite materials' dependability and structural integrity is their stability. The stability of materials under different conditions is evaluated theoretically using structural and dynamic analysis models. Mathematical models based on force balance equations and different load analyses can be used to examine how materials respond until the point of transition or failure. Using theoretical models that connect electrical and mechanical properties, electrostatics investigates how materials react to electric or magnetic fields. This offers a theoretical viewpoint on material interactions in situations where resistance to electrostatic circumstances is necessary [14].

#### C. Durability of Materials and the Impact of Environmental Factors

This element focuses on the interactions of composite materials with environmental elements like humidity, UV light, corrosion, and severe weather. We can forecast the material's lifespan and long-term performance with this viewpoint. In order to give a complete picture of the reasons behind material damage and possible deterioration, theoretical models based on the laws of corrosion and degradation employ equations that explain how qualities change over time. For instance, statistical and predictive models of material durability based on theoretical data are used to assess a material's resistance to weathering using chemical and physical corrosion theory [14].

In order to analyze and comprehend the non-mechanical features of composite materials, models and theories are essential. We can now forecast how materials will behave under different functional settings thanks to this theoretical understanding, which improves our capacity to make corrections and create analytical design and engineering strategies that guarantee better performance, stability, and durability across a range of engineering applications.

### 5. Theories on the Behavior of Composite Materials

Expanding theoretical frameworks and making precise predictions on the design and deployment of composite materials in engineering applications require an understanding of their behavior. The fundamental theories that describe how composite materials behave under different loading scenarios are covered in this section, with an emphasis on analytical and predictive models that are grounded in theoretical mathematics and scientific principles. The function of hypotheses in establishing the boundaries and effectiveness of models is also reviewed, as is the significance of these ideas in creating design approaches that align with the real-world behavior of materials.

#### A. Fundamental Theories for Material Behavior Modeling

The mathematical and scientific basis for understanding and forecasting the behavior of composite materials is represented by basic theories. These theories include continuum mechanics, statistical mechanics, plasticity theory, and communication models between the material's different constituent parts. One essential pillar is Composite Material Theory, which offers a mathematical framework that connects the characteristics of the fibers and matrix and establishes how they interact with one another under different loads. By making certain assumptions about the material's characteristics and mechanical behavior, finite element analysis (FEM) is also used to estimate the material's response under varied load situations [15].

#### B. Models for Analysis and Prediction under Various Load Situations

The behavior of composite materials under mechanical, thermal, and environmental loads is described by mathematical models and theories. These consist of models for flexural, tensile, and compression decomposition; they are predicated on force balancing equations and presumptions on component homogeneity and fiber-matrix interaction characteristics. For instance, the behavior of materials under dynamic loads and the likelihood of long-term cracking or failure are predicted using material failure analysis based on stress-strain theory. In order to forecast the probability of



corrosion and faults as well as their effect on overall performance, theories that integrate statistical analysis and mechanical models are also used [16].

#### C. The Function of Theories in Models

The accuracy and applicability of models of composite material behavior for real-world applications are determined by basic assumptions. For instance, it's customary to assume that material behavior is linear. In order to facilitate computations and theoretical research, this assumption makes the assumption that the material's response is linear over a specific range of loads. Extreme loading circumstances or severe surroundings, however, would necessitate changing these presumptions or using nonlinear models, which would complicate the research and call for a strong theoretical foundation to evaluate the models' viability [17].

To gain a thorough theoretical understanding that serves as a strong basis for material development and the enhancement of the design of more dependable and efficient structures, it is imperative to simulate the behavior of composite materials using recognized research and theories. This feature is essential for differentiating between ideal models and actual conditions, as well as for directing future engineering choices that are grounded in a careful and exhaustive examination of material behavior.

## 6. Enhancing Mechanical Structure Performance using Composite Materials

One of the main pillars supporting the enhancement of mechanical structure performance is the utilization of composite materials' features. In order to describe the behavior of composite materials and their possible uses, an integrated theoretical approach that blends scientific theories with engineering principles must be adopted. This chapter discusses the theoretical underpinnings of designing mechanical structures that are stronger, lighter, and more resilient. It focuses on how the characteristics of composite materials lead to significant advancements in engineering and design techniques.

#### A. Using Composite Materials to Design Structures from a Theoretical Angle

The theoretical design of structures composed of composite materials relies on mathematical models and analytical theories that explain the interaction of these materials with different operating conditions. These models include determining the ideal fiber distribution within the matrix, estimating structural behavior in terms of tension and strain, as well as load-bearing and durability requirements. The theoretical literature is used to formulate engineering rules that describe the relationships between the mechanical properties of composite materials and the loads imposed on them, with the aim of creating design models that meet safety and efficiency standards without relying on practical tests [18].

#### B. Examining the Theories Underpinning Durability, Strength, and Lightweight

Lightweight and durability are fundamental principles of engineering theory. The theoretical aspect reflects how composite materials can be leveraged to achieve a balance between weight and performance. For example, based on structural analysis theories, fiber distribution and stress distribution can be determined to improve load resistance while reducing the overall weight of structures. Advanced design theories also enhance the understanding of fiber-matrix interaction mechanisms, contributing to the development of structures with unique mechanical properties that ensure long-term performance [19].

#### C. Conceptual Approaches to Difficult Design Issues

Mechanical structural designs require the use of theoretical equations and analyses to address complex problems, such as load gradients, crack interactions, and stress distribution. Mathematical models, such as stress-strain theory, are used to analyze the response of composite materials and predict weaknesses or critical areas in the design. Furthermore, multi-objective theoretical methods and computational principles, such as theoretical dynamics and stability theory, are applied to determine the best engineering solutions that maximize structural performance while adhering to safety and cost constraints [20].

The theoretical aspect highlights the use of composite materials as a key support element in improving the performance of mechanical structures, providing engineers with principles and frameworks that help develop more advanced and flexible designs that meet the performance requirements of diverse operating environments. Adopting theoretical foundations enhances the potential for innovation and development in mechanical engineering, contributing to the realization of structures with superior performance in load resistance, lightness, and durability, while reducing reliance on practical experiments and their associated costs [21].

#### **4. Results and Discussion**

The theoretical findings derived from an examination of the fundamental theories, mathematical models, and concepts determining the properties of composite materials and their applications in enhancing the performance of mechanical structures are presented in this section in a thorough and critical manner. In addition to offering a critical assessment and theoretical justification for the design of structures based on composite materials, this part seeks to advance theoretical knowledge of the mechanical, thermal, and environmental characteristics of these materials.

##### **7.1 Examination of Composite Material Properties from a Theoretical Angle**

Theoretical and mathematical models, including those pertaining to ductility, stress, and strain resistance, as well as moment and bending analysis models, that allow for the prediction of the mechanical behavior of composite materials are examined. Relying on differential equations that explain how stress and strain are distributed among the material components, conventional models that are backed by mathematical and physical principles—such as composite frame theory and composite slab theory—offer a strong foundation for comprehending how composite materials behave under loading.

Theories that clarify the connection between toughness and ductility and production characteristics including connectivity, matrix anisotropy, and fiber dispersion are emphasized in relation to mechanical qualities. Theoretical examination demonstrates that enhancing these qualities necessitates a comprehensive comprehension of the elements influencing material behavior, whether they are associated with the operational environment or the design. Theoretical research based on numerical analysis models supports this.

##### **7.2 Analyzing the Theories Supporting Designs for Composite Structures**

When examining the theories that support the design of mechanical structures made of composite materials, it is evident that mathematical models that enable the simulation of the structure's anticipated performance during operation complement theoretical concepts centered on lightness, strength, and durability. For instance, in order to produce lightweight designs with high resistance, composite material theories are used to forecast stress and strain distributions. These theories rely on crucial assumptions like linear stress distribution and the independence of the material's constituent units.

Theoretical discussions also showed that a comprehensive understanding of fiber-matrix interactions is necessary to improve structural performance. Material behavior models, on the other hand, offer valuable analytical tools for predicting failure or possible improvements based on assumptions about fatigue, heterogeneous stress distribution, and defects, improving the ability to design safer and more effective structures.

### 7.3 Assessing Theories in the Framework of Improving Structural Performance

It was shown by the theoretical review that existing theories offer a strong foundation for creating models that categorize and forecast the performance of composite structures without the need for experimental research. The assumptions of homogeneity and uniformity in component qualities, for example, may need to be updated to satisfy more complicated application needs, particularly under various operational and environmental situations. These concerns, however, call for greater examination and discussion.

Theoretical considerations also suggest that combining mathematical models with design concepts grounded in basic dynamics and material principles is necessary for performance improvement. Prediction accuracy may increase as a result, and more adaptable design principles may be offered to meet the demands of engineering applications.

## 8. Conclusion

The study shows that understanding the potential of composite materials and how they can improve the performance of mechanical structures requires a theoretical investigation of their properties. The findings show that the basic theories and mathematical models offered offer a strong foundation for forecasting how these materials will behave under different loading scenarios and directing design procedures in accordance with industrial, military, and civil performance standards. Furthermore, by using theoretical underpinnings to exploit the properties of composite materials, structures that are lightweight, durable, and resistant to harsh environmental conditions and stresses can be developed, improving performance efficiency and prolonging their service life.

This study is valuable because it offers a strong theoretical framework for upcoming advancements and advances in the field of composite materials. It establishes the groundwork for a more thorough comprehension of the behavioral dynamics of these materials and aids in overcoming the difficulties encountered during the design and implementation processes. Additionally, it gives engineers and researchers a theoretically grounded reference model that aids in the development of more precise and efficient design solutions and encourages additional study to investigate novel avenues and upcoming advancements that improve the fusion of theory and practice.

To sum up, a strong theoretical basis is still necessary to promote technical advancement in this area and is the best way to transform the design and development of cutting-edge, sustainable mechanical structures that satisfy contemporary demands.

**Supplementary Materials:** The following supporting information can be downloaded at: [www.mdpi.com/xxx/s1](http://www.mdpi.com/xxx/s1), Figure S1: title; Table S1: title; Video S1: title.

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